

A NOTES ON MULTI (T,S) -INTUITIONISTIC FUZZY SUBFIELD OF A FIELD

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Abstract. In this paper, we made an attempt to study the algebraic nature of a (T,S) intuitionistic fuzzy subfield of a field.

Keywords: (T,S) - norm, (T,S) -intuitionistic fuzzy subfield.

1. Introduction

After the introduction of fuzzy sets by L.A. Zadeh [24], several researchers explored on the generalization of the concept of fuzzy sets. The concept of intuitionistic fuzzy subset was introduced by K.T. Atanassov [4], as a generalization of the notion of fuzzy set. Azriel Rosenfeld [6] defined a fuzzy groups. The notion of fuzzy subgroups, anti-fuzzy subgroups, fuzzy fields and fuzzy linear spaces was introduced by Biswas. R [8]. In this paper, we introduce the some theorems in (T,S) -intuitionistic fuzzy subfield of a field.

2. Preliminaries

Definition 2.1.

A (T,S) -norm is a binary operations $T: [0, 1] \times [0, 1] \rightarrow [0, 1]$ and $S: [0, 1] \times [0, 1] \rightarrow [0, 1]$ satisfying the following requirements;

- (i) $T(0,x) = 0, T(1,x) = x$ (boundary condition)
- (ii) $T(x,y) = T(y,x)$ (commutativity)
- (iii) $T(x,T(y,z)) = T(T(x,y),z)$ (associativity)
- (iv) if $x \leq y$ and $w \leq z$, then $T(x,w) \leq T(y,z)$ (monotonicity).
- (v) $S(0,x) = x, S(1,x) = 1$ (boundary condition)
- (vi) $S(x,y) = S(y,x)$ (commutativity)
- (vii) $S(x,S(y,z)) = S(S(x,y),z)$ (associativity)
- (viii) if $x \leq y$ and $w \leq z$, then $S(x,w) \leq S(y,z)$ (monotonicity).

Definition 2.2. [24]

Let X be a non-empty set. A fuzzy subset A of X is a function $A : X \rightarrow [0, 1]$.

Definition 2.3.

A **multi fuzzy subset** A of a set X is defined as an object of the form $A = \{hx, A_1(x), A_2(x), A_3(x), \dots, A_n(x) \mid x \in X\}$, where $A_i : X \rightarrow [0, 1]$ for all i . It is denoted as $A = hA_1, A_2, A_3, \dots, A_n i$.

Definition 2.4. [2]

An **intuitionistic fuzzy subset (IFS)** A of a set X is defined as an object of the form $A = \{hx, \mu_A(x), \nu_A(x) \mid x \in X\}$, where $\mu_A : X \rightarrow [0, 1]$ and $\nu_A : X \rightarrow [0, 1]$ define the degree of membership and the degree of non-membership of the element x in X respectively and for every x in X satisfying $0 \leq \mu_A(x) + \nu_A(x) \leq 1$.

Definition 2.5.

A **multi intuitionistic fuzzy subset (MIFS)** A of a set X is defined as an object of the form $A = \{hx, \mu_A(x), \nu_A(x) \mid x \in X\}$, where $\mu_A(x) = (\mu_{A1}(x), \mu_{A2}(x), \dots, \mu_{An}(x))$, $\mu_{Ai} : X \rightarrow [0, 1]$ for all i and $\nu_A(x) = (\nu_{A1}(x), \nu_{A2}(x), \dots, \nu_{An}(x))$, $\nu_{Ai} : X \rightarrow [0, 1]$ for all i , define the degrees of membership and the degrees of non-membership of the element x in X respectively and for every x in X satisfying $0 \leq \mu_{Ai}(x) + \nu_{Ai}(x) \leq 1$ for all i .

Definition 2.6.

Let $(F, +, \cdot)$ be a field. An intuitionistic multi fuzzy subset A of F is said to be a **multi (T, S) -intuitionistic fuzzy subfield** of F if the following conditions are satisfied:

- (i) $\mu_{Ai}(x + y) \geq T(\mu_{Ai}(x), \mu_{Ai}(y))$, for all x, y in F ,
- (ii) $\mu_{Ai}(-x) \geq \mu_{Ai}(x)$, for all x in F ,
- (iii) $\mu_{Ai}(xy) \geq T(\mu_{Ai}(x), \mu_{Ai}(y))$, for all x, y in F ,
- (iv) $\mu_{Ai}(x^{-1}) \geq \mu_{Ai}(x)$, for all $x \neq 0$ in F ,
- (v) $\nu_{Ai}(x + y) \leq S(\nu_{Ai}(x), \nu_{Ai}(y))$, for all x, y in F ,
- (vi) $\nu_{Ai}(-x) \leq \nu_{Ai}(x)$, for all x in F ,
- (vii) $\nu_{Ai}(xy) \leq S(\nu_{Ai}(x), \nu_{Ai}(y))$, for all x, y in F ,
- (viii) $\nu_{Ai}(x^{-1}) \leq \nu_{Ai}(x)$, for all $x \neq 0$ in F and for all i .

Example 2.7. Consider the field $Z_5 = \{0, 1, 2, 3, 4\}$ with addition modulo 5 and multiplication modulo 5 operations. Then $A = \{h0, (0.7, 0.6, 0.5), (0.1, 0.2, 0.3) i, h1, (0.6, 0.5, 0.4), (0.2, 0.4, 0.4) i, h2, (0.6, 0.5, 0.4), (0.2, 0.4, 0.4) i, h3, (0.6, 0.5, 0.4), (0.2, 0.4, 0.4) i, h4, (0.6, 0.5, 0.4), (0.2, 0.4, 0.4) i\}$ is a (T, S) -intuitionistic multi fuzzy subfield of Z_5 .

3. Properties**Theorem 3.1.**

If A and B are any two (T, S) -intuitionistic fuzzy subfields of a field $(F, +, \cdot)$, then their intersection $A \cap B$ is an (T, S) -intuitionistic fuzzy subfield of F .

Proof: Let x and y belong to F and let $C = A \cap B$.

Now: $\mu_C(x - y) = \min\{\mu_{Ai}(x - y), \mu_{Bi}(x - y)\}$

$$\begin{aligned}
&\geq \min\{T(\mu_{A_i}(x), \mu_{A_i}(y)), T(\mu_{B_i}(x), \mu_{B_i}(y))\} \\
&\geq T(\min\{\mu_{A_i}(x), \mu_{B_i}(x)\}, \min\{\mu_{A_i}(y), \mu_{B_i}(y)\}) \\
&= T(\mu_C(x), \mu_C(y)).
\end{aligned}$$

Therefore, $\mu_C(x - y) \geq T(\mu_C(x), \mu_C(y))$ for all x, y in F and

$$\begin{aligned}
\mu_C(xy^{-1}) &= \min\{\mu_{A_i}(xy^{-1}), \mu_{B_i}(xy^{-1})\} \\
&\geq \min\{T(\mu_{A_i}(x), \mu_{A_i}(y)), T(\mu_{B_i}(x), \mu_{B_i}(y))\} \\
&\geq T(\min\{\mu_{A_i}(x), \mu_{B_i}(x)\}, \min\{\mu_{A_i}(y), \mu_{B_i}(y)\}) \\
&= T(\mu_C(x), \mu_C(y)).
\end{aligned}$$

Therefore, $\mu_C(xy^{-1}) \geq T(\mu_C(x), \mu_C(y))$ for all x and $y \neq 0$ in F .

Also

$$\begin{aligned}
v_C(x - y) &= \max\{v_{A_i}(x - y), v_{B_i}(x - y)\} \\
&\leq \max\{S(v_{A_i}(x), v_{A_i}(y)), S(v_{B_i}(x), v_{B_i}(y))\} \\
&\leq S(\max\{v_{A_i}(x), v_{B_i}(x)\}, \max\{v_{A_i}(y), v_{B_i}(y)\}) \\
&= S(v_C(x), v_C(y)).
\end{aligned}$$

Therefore, $v_C(x - y) \leq S(v_C(x), v_C(y))$ for all x and y in F and

$$\begin{aligned}
v_C(xy^{-1}) &= \max\{v_{A_i}(xy^{-1}), v_{B_i}(xy^{-1})\} \\
&\leq \max\{S(v_{A_i}(x), v_{A_i}(y)), S(v_{B_i}(x), v_{B_i}(y))\} \\
&\leq S(\max\{v_{A_i}(x), v_{B_i}(x)\}, \max\{v_{A_i}(y), v_{B_i}(y)\}) \\
&= S(v_C(x), v_C(y)).
\end{aligned}$$

Therefore $v_C(xy^{-1}) \leq S(v_C(x), v_C(y))$ for all x and $y \neq 0$ in F .

Hence $A \cap B$ is an (T, S) -intuitionistic fuzzy subfield of a field F .

Theorem 3.2.

The intersection of a family of (T, S) -intuitionistic fuzzy subfields of a field $(F, +, \cdot)$ is an (T, S) -intuitionistic fuzzy subfield of F .

Proof: Let $\{A_i\}_{i \in I}$ be a family of (T, S) -intuitionistic fuzzy subfields of a field F and $A = \bigcap_{i \in I} A_i$ where $\mu_{A_i}(x) = \inf_{i \in I} \mu_{A_i}(x)$ and $v_{A_i}(x) = \sup_{i \in I} v_{A_i}(x)$. Then for x and y belongs to F , then

$$\begin{aligned}
\mu_A(x - y) &= \inf_{i \in I} \mu_{A_i}(x - y) \\
&\geq \inf_{i \in I} T(\mu_{A_i}(x), \mu_{A_i}(y)) \\
&\geq T(\inf_{i \in I} \mu_{A_i}(x), \inf_{i \in I} \mu_{A_i}(y)) \\
&= T(\mu_A(x), \mu_A(y))
\end{aligned}$$

Therefore, $\mu_A(x - y) \geq T(\mu_A(x), \mu_A(y))$ for all x and y in F and

$$\begin{aligned}
\mu_A(xy^{-1}) &= \inf_{i \in I} \mu_{A_i}(xy^{-1}) \\
&\geq \inf_{i \in I} T(\mu_{A_i}(x), \mu_{A_i}(y)) \\
&\geq T(\inf_{i \in I} \mu_{A_i}(x), \inf_{i \in I} \mu_{A_i}(y)) \\
&= T(\mu_A(x), \mu_A(y)).
\end{aligned}$$

Therefore, $\mu_A(xy^{-1}) \geq T(\mu_A(x), \mu_A(y))$ for all x and $y \neq 0$ in F .

Also,

$$\begin{aligned}
v_A(x - y) &= \sup_{i \in I} v_{A_i}(x - y) \\
&\leq \sup_{i \in I} S(v_{A_i}(x), v_{A_i}(y)) \\
&\leq S(\sup_{i \in I} v_{A_i}(x), \sup_{i \in I} v_{A_i}(y)) \\
&= S(v_A(x), v_A(y)).
\end{aligned}$$

Therefore, $v_{Ai}(x - y) \leq S(v_{Ai}(x), v_{Ai}(y))$ for all x and y in F and

$$\begin{aligned} v_{Ai}(xy^{-1}) &= \sup_{i \in I} v_{Ai}(xy^{-1}) \\ &\leq \sup_{i \in I} S(v_{Ai}(x), v_{Ai}(y)) \\ &\leq S(\sup_{i \in I} v_{Ai}(x), \sup_{i \in I} v_{Ai}(y)) \\ &= S(v_{Ai}(x), v_{Ai}(y)). \end{aligned}$$

Therefore $v_{Ai}(xy^{-1}) \leq S(v_{Ai}(x), v_{Ai}(y))$ for all x and $y \neq 0$ in F .

Hence the intersection of a family of (T, S) -intuitionistic fuzzy subfields of a field F is a (T, S) -intuitionistic fuzzy subfield of F .

Theorem 3.3.

If A is a multi (T, S) -intuitionistic fuzzy subfield of a field $(F, +, \cdot)$, then $2A$ is a multi (T, S) -intuitionistic fuzzy subfield of F .

Proof: Let A be a multi (T, S) -intuitionistic fuzzy subfield of a field F .

Consider $A = \{ \langle x, \mu_{Ai}(x), v_{Ai}(x) \rangle \}$, for all x in F and then $2A = B = \{ \langle x, \mu_{Bi}(x), v_{Bi}(x) \rangle \}$, where $\mu_{Bi}(x) = \mu_{Ai}(x)$, $v_{Bi}(x) = 1 - \mu_{Ai}(x)$. Clearly $\mu_{Bi}(x - y) \geq T(\mu_{Bi}(x), \mu_{Bi}(y))$, for all x and y in F and $\mu_{Bi}(xy^{-1}) \geq T(\mu_{Bi}(x), \mu_{Bi}(y))$ for all x and $y \neq 0$ in F . Since A is a multi (T, S) -intuitionistic fuzzy subfield of F , then $\mu_{Ai}(x - y) \geq T(\mu_{Ai}(x), \mu_{Ai}(y))$ for all x and y in F , which implies that:

$$1 - v_{Bi}(x - y) \geq T((1 - v_{Bi}(x)), (1 - v_{Bi}(y)))$$

which implies that: $v_{Bi}(x - y) \leq 1 - T((1 - v_{Bi}(x)), (1 - v_{Bi}(y))) = S(v_{Bi}(x), v_{Bi}(y))$.

Therefore, $v_{Bi}(x - y) \leq S(v_{Bi}(x), v_{Bi}(y))$ for all x and y in F and $\mu_{Ai}(xy^{-1}) \geq T(\mu_{Ai}(x), \mu_{Ai}(y))$ for all x and $y \neq 0$ in F , which implies that:

$$1 - v_{Bi}(xy^{-1}) \geq T((1 - v_{Bi}(x)), (1 - v_{Bi}(y)))$$

which implies that $v_{Bi}(xy^{-1}) \leq 1 - T((1 - v_{Bi}(x)), (1 - v_{Bi}(y))) = S(v_{Bi}(x), v_{Bi}(y))$.

Therefore, $v_{Bi}(xy^{-1}) \leq S(v_{Bi}(x), v_{Bi}(y))$ for all x and $y \neq 0$ in F .

Hence $B = 2A$ is a multi (T, S) -intuitionistic fuzzy subfield of a field F .

Theorem 3.4.

If A is a multi (T, S) -intuitionistic fuzzy subfield of a field $(F, +, \cdot)$, then $\diamond A$.

Proof: Let A be a multi (T, S) -intuitionistic fuzzy subfield of a field F . That is $A = \{ \langle x, \mu_{Ai}(x), v_{Ai}(x) \rangle \}$, for all x in F . Let $\diamond A = B = \{ \langle x, \mu_{Bi}(x), v_{Bi}(x) \rangle \}$, where $\mu_{Bi}(x) = 1 - v_{Ai}(x)$, $v_{Bi}(x) = v_{Ai}(x)$.

Clearly $v_{Bi}(x - y) \leq S(v_{Bi}(x), v_{Bi}(y))$, for all x and y in F and $v_{Bi}(xy^{-1}) \leq S(v_{Bi}(x), v_{Bi}(y))$ for all x and $y \neq 0$ in F . Since A is a multi (T, S) -intuitionistic fuzzy subfield of F , then $v_{Ai}(x - y) \leq S(v_{Ai}(x), v_{Ai}(y))$ for all x and y in F which implies that $\mu_{Bi}(x - y) \geq 1 - S((1 - \mu_{Bi}(x)), (1 - \mu_{Bi}(y))) = T(\mu_{Bi}(x), \mu_{Bi}(y))$. Therefore, $\mu_{Bi}(x - y) \geq T(\mu_{Bi}(x), \mu_{Bi}(y))$ for all x and y in F and $v_{Ai}(xy^{-1}) \leq S(v_{Ai}(x), v_{Ai}(y))$ for all x and $y \neq 0$ in F , which implies that

$$1 - \mu_{Bi}(xy^{-1}) \leq S((1 - \mu_{Bi}(x)), (1 - \mu_{Bi}(y)))$$

which implies that $\mu_{Bi}(xy^{-1}) \geq 1 - S((1 - \mu_{Bi}(x)), (1 - \mu_{Bi}(y))) = T(\mu_{Bi}(x), \mu_{Bi}(y))$.

Therefore $\mu_{Bi}(xy^{-1}) \geq T(\mu_{Bi}(x), \mu_{Bi}(y))$ for all x and $y \neq 0$ in F .

Hence $B = \diamond A$ is a multi (T, S) -intuitionistic fuzzy subfield of a field F .

Theorem 3.5.

If A and B are multi (T, S) -intuitionistic fuzzy subfields of the fields G and H respectively, then $A \times B$ is an multi (T, S) -intuitionistic fuzzy subfield of $G \times H$.

Proof: Let A and B be multi (T, S) -intuitionistic fuzzy subfields of the fields G and H respectively.

Let x_1 and x_2 be in G , y_1 and y_2 be in H . Then (x_1, y_1) and (x_2, y_2) are in $G \times H$. Now,

$$\begin{aligned} \mu_{A \times B}[(x_1, y_1) - (x_2, y_2)] &= \mu_{A \times B}(x_1 - x_2, y_1 - y_2) \\ &= \min\{\mu_{Ai}(x_1 - x_2), \mu_{Bi}(y_1 - y_2)\} \end{aligned}$$

$$\begin{aligned}
&\geq \min \{T(\mu_{A_i}(x_1), \mu_{A_i}(x_2)), T(\mu_{B_i}(y_1), \mu_{B_i}(y_2))\} \\
&\geq T(\min(\mu_{A_i}(x_1), \mu_{B_i}(y_1)), \min(\mu_{A_i}(x_2), \mu_{B_i}(y_2))) \\
&= T(\mu_{A_i \times B_i}(x_1, y_1), \mu_{A_i \times B_i}(x_2, y_2)).
\end{aligned}$$

Therefore,

$$\mu_{A_i \times B_i}[(x_1, y_1) - (x_2, y_2)] \geq T(\mu_{A_i \times B_i}(x_1, y_1), \mu_{A_i \times B_i}(x_2, y_2)), \text{ for all } x_1 \text{ and } x_2 \text{ in } G \text{ and } y_1 \text{ and } y_2 \text{ in } H.$$

$$\text{Now, } \mu_{A_i \times B_i}[(x_1, y_1)(x_2, y_2)^{-1}] = \mu_{A_i \times B_i}(x_1 x^{-21}, y_1 y_2^{-1})$$

$$\begin{aligned}
&= \min \{ \mu_{A_i}(x_1 x^{-21}), \mu_{B_i}(y_1 y_2^{-1}) \} \\
&\geq \min \{ T(\mu_{A_i}(x_1), \mu_{A_i}(x_2)), T(\mu_{B_i}(y_1), \mu_{B_i}(y_2)) \} \\
&\geq T(\min(\mu_{A_i}(x_1), \mu_{B_i}(y_1)), \min(\mu_{A_i}(x_2), \mu_{B_i}(y_2))) \\
&= T(\mu_{A_i \times B_i}(x_1, y_1), \mu_{A_i \times B_i}(x_2, y_2)).
\end{aligned}$$

Therefore, $\mu_{A_i \times B_i}[(x_1, y_1)(x_2, y_2)^{-1}] \geq T(\mu_{A_i \times B_i}(x_1, y_1), \mu_{A_i \times B_i}(x_2, y_2))$, for all x_1 and $x_2 = 06$ in G and y_1 and y_2

$$6 = 0^0 \text{ in } H \text{ and, } v_{A_i \times B_i}[(x_1, y_1) - (x_2, y_2)] = v_{A_i \times B_i}(x_1 - x_2, y_1 - y_2)$$

$$\begin{aligned}
&= \max \{ v_{A_i}(x_1 - x_2), v_{B_i}(y_1 - y_2) \} \\
&\leq \max \{ S(v_{A_i}(x_1), v_{A_i}(x_2)), S(v_{B_i}(y_1), v_{B_i}(y_2)) \} \\
&\leq S(\max(v_{A_i}(x_1), v_{B_i}(y_1)), \max(v_{A_i}(x_2), v_{B_i}(y_2))) \\
&= S(v_{A_i \times B_i}(x_1, y_1), v_{A_i \times B_i}(x_2, y_2)).
\end{aligned}$$

Therefore, $v_{A_i \times B_i}[(x_1, y_1) - (x_2, y_2)] \leq S(v_{A_i \times B_i}(x_1, y_1), v_{A_i \times B_i}(x_2, y_2))$, for all x_1 and x_2 in G and y_1 and y_2 in H

$$\text{and } v_{A_i \times B_i}[(x_1, y_1)(x_2, y_2)^{-1}] = v_{A_i \times B_i}(x_1 x^{-21}, y_1 y_2^{-1})$$

$$\begin{aligned}
&= \max \{ v_{A_i}(x_1 x^{-21}), v_{B_i}(y_1 y_2^{-1}) \} \\
&\leq \max \{ S(v_{A_i}(x_1), v_{A_i}(x_2)), S(v_{B_i}(y_1), v_{B_i}(y_2)) \} \\
&\leq S(\max(v_{A_i}(x_1), v_{B_i}(y_1)), \max(v_{A_i}(x_2), v_{B_i}(y_2))) \\
&= S(v_{A_i \times B_i}(x_1, y_1), v_{A_i \times B_i}(x_2, y_2)).
\end{aligned}$$

Therefore, $v_{A_i \times B_i}[(x_1, y_1)(x_2, y_2)^{-1}] \leq S(v_{A_i \times B_i}(x_1, y_1), v_{A_i \times B_i}(x_2, y_2))$, for all x_1 and $x_2 = 06$ in G and y_1 and $y_2 = 0^0$ in H .

Hence $A \times B$ is an multi (T, S) -intuitionistic fuzzy subfield of $G \times H$.

References

- [1] Akram.M and K.H.Dar, *On Anti Fuzzy Left h-ideals in Hemirings*, International Mathematical Forum, **2**(46), (2007), 2295 - 2304.
- [2] Anthony.J.M. and H Sherwood, *Fuzzy groups Redefined*, Journal of mathematical analysis and applications, **69**, (1979), 124 -130.
- [3] AsokKumer Ray, *On product of fuzzy subgroups*, Fuzzy Sets and Systems, **105**, (1999), 181-183.
- [4] Atanassov.K.T., *Intuitionistic fuzzy sets*, Fuzzy Sets and Systems, **20**(1), (1986), 87-96.
- [5] Atanassov.K.T., *Intuitionistic fuzzy sets theory and applications*, Physica-Verlag, A Springer-Verlag Company, Bulgaria, (1999).
- [6] Azriel Rosenfeld, *Fuzzy Groups*, Journal of Mathematical Analysis and Applications, **35**, (1971), 512-517.
- [7] Banerjee.B and D.K.Basnet, *Intuitionistic fuzzy subrings and ideals*, J. Fuzzy Math., **11**(1), (2003), 139-155.
- [8] Biswas.R, *Fuzzy subgroups and Anti-fuzzy subgroups*, Fuzzy Sets and Systems, **35**, (1990), 121-124.
- [9] Chakrabarty, K., Biswas and R., Nanda, *A note on union and intersection of Intuitionistic fuzzy sets*, Notes on Intuitionistic Fuzzy Sets, **3**(4), (1997).
- [10] Choudhury. F.P, A.B. Chakraborty and S.S. Khare, *A note on fuzzy subgroups and fuzzy homomorphism*, Journal of Mathematical Analysis and Applications, **131**, (1988), 537-553.
- [11] De, K., R.Biswas and A.R.Roy, *On intuitionistic fuzzy sets*, Notes on Intuitionistic Fuzzy Sets, text**3**(4), (1997).
- [12] Hur.K, H.W Kang and H.K.Song, *Intuitionistic fuzzy subgroups and subrings*, Honam Math. J., **25**(1), (2003), 19-41.
- [13] Hur.K, S.Y Jang and H.W Kang, *(T,S)-intuitionistic fuzzy ideals of a ring*, J. Korea Soc. Math. Educ. Ser. B: Pure Appl. Math., **12**(3), (2005), 193-209.
- [14] Jianming Zhan, *On Properties of Fuzzy Left h-Ideals in Hemiring with t-Norms*, International Journal of Mathematical Sciences, **19**, (2005), 3127-3144.
- [15] Jun. Y.B, M.A Ozturk and C.H. Park, *Intuitionistic nil radicals of (T,S)-intuitionistic fuzzy ideals and Euclidean (T,S)-intuitionistic fuzzy ideals in rings*, Inform. Sci., **177**, (2007), 4662-4677.

- [16] Mustafa Akgul, *Some properties of fuzzy groups*, Journal of Mathematical Analysis and Applications, **133**, (1988), 93-100.
- [17] Palaniappan. N and K. Arjunan, *The homomorphism, anti homomorphism of a fuzzy and an anti fuzzy ideals of a ring*, Varahmihir Journal of Mathematical Sciences, **6(1)**, (2008), 181-186.
- [18] Palaniappan. N and K. Arjunan, *Operation on fuzzy and anti fuzzy ideals*, Antarctica J. Math., **4(1)**, (2007), 59-64.
- [19] Palaniappan. N and K. Arjunan, *Some properties of intuitionistic fuzzy subgroups*, Acta Ciencia Indica, **XXXIII(2)**, (2007), 321-328.
- [20] Rajesh Kumar, *Fuzzy irreducible ideals in rings*, Fuzzy Sets and Systems, **42**, (1991), 369-379.
- [21] Rajesh Kumar, *Fuzzy Algebra*, University of Delhi Publication Division, **1**, (1993).
- [22] Sivaramakrishnas.P, *Fuzzy groups and level subgroups*, Journal of Mathematical Analysis and Applications, **84**, (1981), 264-269.
- [23] Vasantha Kandasamy. W.B, *Smarandache fuzzy algebra*, American Research Press, Rehoboth, (2003).
- [24] Zadeh .L.A, *Fuzzy sets*, Information and Control, **8**, (1965), 338-353.