

Further results on super exponential mean graphs

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Abstract Let G be a graph and $f: V(G) \to \{1, 2, 3, ..., p + q\}$ be an injection. For each uv, the induced edge labeling f^* is defined as

$$\chi^*(uv) = \left[\frac{1}{e} \left(\frac{\chi(v)^{\chi(v)}}{\chi(u)^{\chi(u)}}\right)^{\frac{1}{\chi(v)-\chi(u)}}\right].$$

Then f is called a super exponential mean labeling if $f(V(G)) \cup \{f^*(uv): uv \in E(G)\} = \{1,2,3,..., p+q\}$. A graph that admits a super exponential mean labeling is called a super exponential mean graph. In this paper, we have discussed the super exponential meanness of some standard graphs.

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1. Introduction

In this paper, only finite, simple and undirected graphs are considered. For terminology, definitions we follow [7] and for survey [6].

A path on *n* vertices is denoted by P_n . The graph $\hat{G}(p_1, m_1, p_2, m_2, ..., m_{n-1}, p_n)$ is obtained from *n* cycles of length $p_1, p_2, ..., p_n$ and (n-1) paths on $m_1, m_2, ..., m_{n-1}$ vertices respectively by identifying a cycle and a path at a vertex alternatively as follows: If the j^{th} cycles is of odd length, then its $\left(\frac{p_j+2}{2}\right)^{th}$ vertex is identified with a pendant vertex of j^{th} path and if the j^{th} cycle is of even length, then its $\left(\frac{p_j+2}{2}\right)^{th}$ vertex is identified with a pendant vertex of j^{th} path while the other pendant vertex of the j^{th} path is identified with the first vertex of the $(j+1)^{th}$ cycle. The graph $G^*(p_1, p_2, ..., p_n)$ is obtained from *n* cycles of length $p_1, p_2, ..., p_n$ by identifying consecutive cycles at a vertex as follows. If the j^{th} cycle is of odd length, then its $\left(\frac{p_j+3}{2}\right)^{th}$ vertex is identified with the first vertex of $(j+1)^{th}$ cycle and if the j^{th} cycle is of even length, then its $\left(\frac{p_j+2}{2}\right)^{th}$ vertex is identified with the first with the first vertex of $(j + 1)^{th}$ cycle. The graph Tadpoles T(n, k) is obtained by identifying a vertex of the cycle C_n to an end vertex of the path P_k . The triangular ladder $TL_n, n \ge 2$ is a graph obtained by completing the ladder L_n by the edges $u_i v_{i+1}$ for $1 \le i \le n - 1$, where L_n is the graph $P_2 \times P_n$.

 $P_2 \times P_n$. The middle graph M(G) of a graph G is the graph whose vertex set is $\{v: v \in V(G)\} \cup \{e: e \in E(G)\}$ and the edge set is $\{e_1e_2: e_1, e_2 \in E(G)\}$ and e_1 and e_2 are adjacent edges of $G\} \cup \{ve: v \in V(G), e \in E(G)\}$ and e is incident with $v\}$. The total graph T(G) of a graph G is the graph whose vertex set is $V(G) \cup E(G)$ and two vertices are adjacent if and only if either they are adjacent vertices of G or adjacent edges of G or one is a vertex of G and the other one is an edge incident on it. A twig $TW(P_n), n \ge 3$ is a graph obtained from a path by attaching exactly two pendant vertices to each internal vertices of the path.

The concept of exponential mean labeling was introduced [1] and developed the exponential mean labeling of some standard graphs [2] by by Rajesh Kannan et al.. The concept of super geometric labeling was first introduced by Durai Baskar et al. [3]. Arockiaraj et al. introduced the super F-root square mean labeling of graphs [4]. Rajesh Kannan et al. introduced super exponential mean labeling of graphs [5]. Motivated by the works on graph labeling, we discussed the further results on super exponential mean labeling of some standard graphs.

Let G be a graph and $f: V(G) \rightarrow \{1, 2, 3, ..., p + q\}$ be an injection. For each uv, the induced edge labeling f^* is defined as

$$\chi^*(uv) = \left[\frac{1}{e} \left(\frac{\chi(v)\chi(v)}{\chi(u)\chi(u)}\right)^{\frac{1}{\chi(v)-\chi(u)}}\right]$$

Then f is called a super exponential mean labeling if $f(V(G)) \cup \{f^*(uv): uv \in E(G)\} = \{1,2,3,..., p+q\}$. A graph that admits a super exponential mean labeling is called a super exponential mean graph.



Figure 1. A super exponential mean labeling of C_4

2. Main Results

Theorem 2.1 $\widehat{G}(p_1, k_1, p_2, k_2, ..., k_{n-1}, p_n)$ is a super exponential mean graph with $p_{\alpha} \neq 4$ for $2 \leq \alpha \leq n$ and for any k_{α} .

Proof. Let $\{v_{\beta}^{(\alpha)}: 1 \le \alpha \le n \text{ and } 1 \le \beta \le p_{\alpha}\}$ be the vertices of the *n* number of cycles in \hat{G} with $p_{\alpha} \ne 4$ for $2 \le \alpha \le n$.

Let $\{u_{\beta}^{(\alpha)}: 1 \le \alpha \le n-1 \text{ and } 1 \le \beta \le k_{\alpha}\}$ be the vertices of the (n-1) number of paths in \hat{G} . For $1 \le \alpha \le n-1$, the α^{th} cycle and α^{th} path are identified by a vertex $v_{\left(\frac{p_{\alpha}+3}{2}\right)}^{(\alpha)}$ and $u_{1}^{(\alpha)}$ while p_{α} is odd and $v_{\left(\frac{p_{\alpha}+2}{2}\right)}^{(\alpha)}$ and $u_{1}^{(\alpha)}$ while p_{α} is even and the α^{th} path and the $(\alpha + 1)^{th}$ cycle are identified by a vertex $u_{k_{\alpha}}^{(\alpha)}$ and $v_{1}^{(\alpha+1)}$ in \hat{G} .

Define $f: V(\hat{G}) \rightarrow \{1, 2, 3, \dots, \sum_{\alpha=1}^{n-1} (2p_{\alpha} + 2k_{\alpha}) + 2p_n - 3n + 3\}$ as follows: When p_1 is odd,

$$\begin{pmatrix} u_{\beta}^{(1)} \end{pmatrix} = f\left(v_{\left\lfloor \frac{p_{1}}{2} \right\rfloor + 2}^{(1)}\right) + 2\beta - 2, \text{ for } 2 \le \beta \le k_{1} \text{ and}$$

$$f\left(v_{\beta}^{(1)}\right) = \begin{cases} 1 & \beta = 1 \\ 4\beta - 4 & 2 \le \beta \le \left\lfloor \frac{p_{1}}{2} \right\rfloor \\ 4\beta - 5 & \beta = \left\lfloor \frac{p_{1}}{2} \right\rfloor + 1 \\ 4\beta - 6 & \beta = \left\lfloor \frac{p_{1}}{2} \right\rfloor + 2 \\ 4p_{1} + 5 - 4\beta & \left\lfloor \frac{p_{1}}{2} \right\rfloor + 3 \le j \le p_{1}. \end{cases}$$

The induced edge labeling is as follows:

$$f^{*}\left(v_{\beta}^{(1)}v_{\beta+1}^{(1)}\right) = \begin{cases} 4\beta - 2 & 1 \leq \beta \leq \left\lfloor\frac{p_{1}}{2}\right\rfloor \\ 4\beta - 3 & \beta = \left\lfloor\frac{p_{1}}{2}\right\rfloor + 1 \\ 4\beta - 8 & \beta = \left\lfloor\frac{p_{1}}{2}\right\rfloor + 2 \\ 4p_{1} + 3 - 4\beta & \left\lfloor\frac{p_{1}}{2}\right\rfloor + 3 \leq \beta \leq p_{1} - 1, \end{cases}$$

$$f^* \left(v_1^{(1)} v_{p_1}^{(1)} \right) = 3 \text{ and}$$

$$f^* \left(u_{\beta}^{(1)} u_{\beta+1}^{(1)} \right) = f \left(v_{\lfloor \frac{p_1}{2} \rfloor + 2}^{(1)} \right) + 2\beta - 1, \text{ for } 1 \le \beta \le k_1 - 1.$$
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When p_1 is even,

f

$$f\left(v_{\beta}^{(1)}\right) = \begin{cases} 1 & \beta = 1 \\ 4\beta - 4 & 2 \le \beta \le \left\lfloor\frac{p_{1}}{2}\right\rfloor + 1 \\ 4p_{1} + 5 - 4\beta & \left\lfloor\frac{p_{1}}{2}\right\rfloor + 2 \le \beta \le p_{1} \text{ and} \end{cases}$$
$$f\left(u_{\beta}^{(1)}\right) = f\left(v_{\lfloor\frac{p_{1}}{2}\rfloor+1}^{(1)}\right) + 2\beta - 2, \text{ for } 2 \le \beta \le k_{1}.$$

The induced edge labeling is as follows:

$$f^*\left(v_{\beta}^{(1)}v_{\beta+1}^{(1)}\right) = \begin{cases} 4\beta - 2 & 1 \le \beta \le \left\lfloor\frac{p_1}{2}\right\rfloor \\ 4p_1 + 3 - 4\beta & \left\lfloor\frac{p_1}{2}\right\rfloor + 1 \le \beta \le p_1 - 1, \end{cases}$$

$$f^*\left(v_1^{(1)}v_{\beta+1}^{(1)}\right) = 3 \text{ and}$$

$$f^*\left(u_{\beta}^{(1)}u_{\beta+1}^{(1)}\right) = f\left(v_{\left\lfloor\frac{p_1}{2}\right\rfloor + 1}^{(1)}\right) + 2\beta - 1, \text{ for } 1 \le \beta \le k_1 - 1.$$
For $2 \le i \le n - 1$,

$$f\left(u_{\beta}^{(\alpha)}\right) = \begin{cases} f\left(v_{\left\lfloor\frac{p_{\alpha}}{2}\right\rfloor + 2}\right) + 2\beta - 2 & 2 \le \beta \le k_i \text{ and } p_{\alpha} \text{ is odd } 1mm \\ f\left(v_{\left\lfloor\frac{p_{\alpha}}{2}\right\rfloor + 1}\right) + 2\beta - 2 & 2 \le \beta \le k_{\alpha} \text{ and } p_{\alpha} \text{ is even.} \end{cases}$$
For $2 \le i \le n$,

$$f\left(v_{\beta}^{(\alpha)}\right) = \begin{cases} \left(f\left(u_{k_{\alpha-1}}^{(\alpha-1)}\right) + 4\beta - 6 & 2 \leq \beta \leq \left\lfloor\frac{p_{\alpha}}{2}\right\rfloor + 1 \text{ and } p_{\alpha} \text{ is odd } 1mm \\ f\left(u_{k_{\alpha-1}}^{(\alpha-1)}\right) + 4p_{\alpha} + 5 - 4\beta & \left\lfloor\frac{p_{\alpha}}{2}\right\rfloor + 2 \leq \beta \leq p_{\alpha} \text{ and } p_{\alpha} \text{ is odd} \end{cases} \\ \begin{cases} f\left(u_{k_{\alpha-1}}^{(\alpha-1)}\right) + 4\beta - 6 & 2 \leq \beta \leq \left\lfloor\frac{p_{\alpha}}{2}\right\rfloor \text{ and } p_{\alpha} \text{ is even } 1mm \\ f\left(u_{k_{\alpha-1}}^{(\alpha-1)}\right) + 4\beta - 5 & \beta = \left\lfloor\frac{p_{\alpha}}{2}\right\rfloor + 1 \text{ and } p_{\alpha} \text{ is even } 1mm \\ f\left(u_{k_{\alpha-1}}^{(\alpha-1)}\right) + 4\beta - 12 & \beta = \left\lfloor\frac{p_{\alpha}}{2}\right\rfloor + 2 \text{ and } p_{\alpha} \text{ is even } 1mm \\ f\left(u_{k_{\alpha-1}}^{(\alpha-1)}\right) + 4p_{\alpha} + 5 - 4\beta & \left\lfloor\frac{p_{\alpha}}{2}\right\rfloor + 3 \leq \beta \leq p_{\alpha} \\ \text{ and } p_{\alpha} \text{ is even.} \end{cases}$$

The induced edge labeling is as follows: For $2 \le \alpha \le n$,

$$f^{*}(v_{\beta}^{(\alpha)}v_{\beta+1}^{(\alpha)}) = \begin{cases} \begin{pmatrix} f(u_{k_{\alpha-1}}^{(\alpha-1)}) + 1 & \beta = 1 \text{ and } p_{\alpha} \text{ is odd } 2mm \\ f(u_{k_{\alpha-1}}^{(\alpha-1)}) + 4\beta - 4 & 2 \leq \beta \leq \left\lfloor \frac{p_{\alpha}}{2} \right\rfloor + 1 \\ \text{and } p_{\alpha} \text{ is odd } 2mm & 2mm \\ f(u_{k_{\alpha-1}}^{(\alpha-1)}) + 4p_{\alpha} + 3 - 4\beta & \left\lfloor \frac{p_{\alpha}}{2} \right\rfloor + 2 \leq \beta \leq p_{\alpha} - 1 \\ \text{and } p_{\alpha} \text{ is odd} \\ f(u_{k_{\alpha-1}}^{(\alpha-1)}) + 1 & \beta = 1 \text{ and } p_{\alpha} \text{ is even } 2mm \\ f(u_{k_{\alpha-1}}^{(\alpha-1)}) + 4\beta - 4 & 2 \leq \beta \leq \left\lfloor \frac{p_{\beta}}{2} \right\rfloor - 1 \\ \text{and } p_{\alpha} \text{ is even } 2mm \\ f(u_{k_{\alpha-1}}^{(\alpha-1)}) + 4\beta - 3 & \beta = \left\lfloor \frac{p_{\alpha}}{2} \right\rfloor \\ \text{and } p_{\alpha} \text{ is even } 2mm \\ f(u_{k_{\alpha-1}}^{(\alpha-1)}) + 4\beta - 6 & \beta = \left\lfloor \frac{p_{\alpha}}{2} \right\rfloor + 1 \\ \text{and } p_{\alpha} \text{ is even } 2mm \\ f(u_{k_{\alpha-1}}^{(\alpha-1)}) + 4\beta - 6 & \beta = \left\lfloor \frac{p_{\alpha}}{2} \right\rfloor + 1 \\ \text{and } p_{\alpha} \text{ is even } 2mm \\ f(u_{k_{\alpha-1}}^{(\alpha-1)}) + 4p_{\alpha} + 3 - 4\beta & \left\lfloor \frac{p_{\alpha}}{2} \right\rfloor + 2 \leq j \leq p_{\alpha} - 1 \\ \text{and } p_{\alpha} \text{ is even,}, \end{cases}$$

For $2 \le i \le n - 1$,

$$f^*\left(v_1^{(\alpha)}v_{p_{\alpha}}^{(\alpha)}\right) = f\left(u_{k_{\alpha-1}}^{(\alpha-1)}\right) + 3 \text{ and}$$

$$f^*\left(u_{\beta}^{(\alpha)}u_{\beta+1}^{(\alpha)}\right) = \begin{cases} f\left(v_{\lfloor\frac{p_{\alpha}}{2}\rfloor+2}^{(\alpha)}\right) + 2\beta - 1 & 1 \le \beta \le k_{\alpha} - 1 \text{ and } p_{\alpha} \text{ is odd } 2mm \\ f\left(v_{\lfloor\frac{p_{\alpha}}{2}\rfloor+1}^{(\alpha)}\right) + 2\beta - 1 & 1 \le \beta \le k_{\alpha} - 1 \text{ and } p_{\alpha} \text{ is even.} \end{cases}$$

Hence, f is a super exponential mean labeling of $\hat{G}(p_1, k_1, p_2, k_2, \dots, k_{n-1}, p_n)$. Thus the graph $\hat{G}(p_1, k_1, p_2, k_2, \dots, k_{n-1}, p_n)$ is a super exponential mean graph with $p_i \neq 4$ for $2 \leq i \leq n$ and for any k_i .

Corollary 2.2 $G^*(p_1, p_2, ..., p_n)$ is a super exponential mean graph with $p_i \neq 4$, for all $2 \le i \le n$. *Corollary 2.3* Every triangular snake is a super exponential mean graph.

Corollary 2.4 Tadpoles T(n, k) is a super exponential mean graph, for $n \ge 3$ and $k \ge 2$.

Theorem 2.5 TL_n is a super exponential mean graph, for $n \ge 3$.

Proof. Let the vertex set of TL_n be $\{v_1, v_2, ..., v_n, u_1, u_2, ..., u_n\}$ and the edge set of TL_n be $\{u_\alpha u_{i+1}, u_i v_{\alpha+1}, v_\alpha v_{\alpha+1}: 1 \le i \le n-1\} \cup \{u_\alpha v_\alpha: 1 \le \alpha \le n\}$. Then TL_n has 2n vertices and 4n-3 edges. Define $f: V(TL_n) \to \{1, 2, 3, ..., 6n-3\}$ as follows:

$$f(v_{\alpha}) = \begin{cases} 1 & \alpha = 1 \\ 6\alpha - 6 & 2 \le \alpha \le n, \\ f(u_{\alpha}) = 6\alpha - 2 \text{ for } 1 \le \alpha \le n - 1 \end{cases}$$

and $f(u_n) = 6n - 3$.

The induced edge labeling is as follows:

 $f^*(v_{\alpha}v_{\alpha+1}) = 6\alpha - 3 \text{ for } 1 \le \alpha \le n - 1,$ $f^*(u_{\alpha}u_{\alpha+1}) = 6\alpha + 1 \text{ for } 1 \le \alpha \le n - 1,$ $f^*(u_{\alpha}v_{\alpha}) = 6\alpha - 4 \text{ for } 1 \le \alpha \le n \text{ and}$ $f^*(u_{\alpha}v_{\alpha+1}) = 6\alpha - 1 \text{ for } 1 \le \alpha \le n - 1.$

Hence, *f* is a super exponential mean labeling of TL_n . Thus the graph TL_n is a super exponential mean graph for $n \ge 3$.

Theorem 2.6 $M(P_n)$ is a super exponential mean graph, for $n \ge 4$.

Proof. Let $V(P_n) = \{v_1, v_2, ..., v_n\}$ and $E(P_n) = \{e_\alpha = v_\alpha v_{\alpha+1} : 1 \le \alpha \le n-1\}$ be the vertex set and edge set of the path P_n . Then

 $V(M(P_n)) = \{v_1, v_2, ..., v_n, e_1, e_2, ..., e_{n-1}\} \text{ and } E(M(P_n)) = \{v_{\alpha}e_{\alpha}, e_{\alpha}v_{\alpha+1}: 1 \le \alpha \le n-1\} \cup \{e_{\alpha}e_{\alpha+1}: 1 \le \alpha \le n-2\}.$ Define $f: V(M(P_n)) \to \{1, 2, 3, ..., 5n-5\}$ as follows:

$$f(v_{\alpha}) = \begin{cases} 1 & i = 1 \\ 2\alpha + 1 & 2 \le \alpha \le 3 \\ 5\alpha - 5 & 4 \le \alpha \le n \text{ and} \\ f(e_{\alpha}) = \begin{cases} 8\alpha - 5 & 1 \le \alpha \le 2 \\ 5\alpha - 2 & 3 \le \alpha \le n - 1. \end{cases}$$

The induced edge labeling is as follows:

$$f^{*}(e_{\alpha}e_{\alpha+1}) = \begin{cases} 6\alpha & 1 \le \alpha \le 2\\ 5\alpha+1 & 3 \le \alpha \le n-2, \end{cases}$$
$$f^{*}(e_{\alpha}v_{\alpha}) = \begin{cases} 2\alpha+4 & 2 \le \alpha \le 3\\ 2\alpha+4 & 2 \le \alpha \le 3\\ 5i-3 & 4 \le \alpha \le n-1 \end{cases}$$

and $f^*(e_{\alpha}v_{\alpha+1}) = 5i - 1$ for $1 \le \alpha \le n - 1$. Hence, f is a super exponential mean labeling of $M(P_n)$. Thus the graph $M(P_n)$ is a super exponential mean graph for $n \ge 4$.

Theorem 2.7 The total graph $T(P_n)$ is a super exponential mean graph, for $n \ge 2$.

Proof. Let $V(P_n) = \{v_1, v_2, ..., v_n\}$ and $E(P_n) = \{e_\alpha = v_\alpha v_{\alpha+1} : 1 \le \alpha \le n-1\}$ be the vertex set and edge set of the path P_n . Then

 $V(T(P_n)) = \{v_1, v_2, \dots, v_n, e_1, e_2, \dots, e_{n-1}\} \text{ and } E(T(P_n)) = \{v_\alpha, v_{\alpha+1}, e_\alpha v_\alpha, e_\alpha v_{\alpha+1}: 1 \le \alpha \le n-1\} \cup \{e_\alpha e_{\alpha+1}: 1 \le \alpha \le n-2\}.$ Define $f: V(T(P_n)) \to \{1, 2, 3, \dots, 6n-6\}$ as follows: $f(v_\alpha) = \begin{cases} 1 & i = 1 \\ 6\alpha - 6 & 2 \le \alpha \le n \text{ and} \end{cases}$ $f(e_\alpha) = 6\alpha - 2, \text{ for } 1 \le \alpha \le n-1.$

The induced edge labeling is as follows: $f^*(v_{\alpha}v_{\alpha+1}) = 6i - 3, \text{ for } 1 \le \alpha \le n - 1,$ $f^*(e_{\alpha}v_{\alpha}) = 6\alpha - 4, \text{ for } 1 \le \alpha \le n - 1,$ $f^*(e_{\alpha}v_{\alpha+1}) = 6\alpha - 1, \text{ for } 1 \le \alpha \le n - 1 \text{ and}$ $f^*(e_{\alpha}e_{\alpha+1}) = 6\alpha + 1, \text{ for } 1 \le \alpha \le n - 2.$

Hence, f is a super exponential mean labeling of $T(P_n)$. Thus the graph $T(P_n)$ is a super exponential mean graph, for $n \ge 2$.

Theorem 2.8 TW(P_n) is a super exponential mean graph, for $n \ge 3$.

Proof. Let $u_1, u_2, ..., u_n$ be the vertices of the path P_n and $v_1^{(\alpha)}, v_2^{(\alpha)}$ be the pendant vertices at each vertex u_{α} of the path P_n , for $2 \le \alpha \le n - 1$. Then

$$V(TW(P_n)) = V(P_n) \cup \left\{ v_1^{(\alpha)}, v_2^{(\alpha)} : 2 \le \alpha \le n - 1 \right\} \text{ and}$$

$$E(TW(P_n)) = E(P_n) \cup \left\{ u_\alpha v_1^{(\alpha)}, u_\alpha v_2^{(\alpha)} : 2 \le \alpha \le n - 1 \right\}.$$
Define $f: V(TW(P_n)) \to \{1, 2, 3, ..., 6n - 9\}$ as follows:

$$f(u_\alpha) = \begin{cases} 1 & \alpha = 1 \\ 6\alpha - 7 & 2 \le \alpha \le n - 2, \\ f(u_{n-1}) = 6n - 11, f(u_n) = 6n - 9, \\ f\left(v_1^{(\alpha)}\right) = \begin{cases} 2 & \alpha = 2 \\ 6\alpha - 9 & 3 \le \alpha \le n - 2, \\ f\left(v_1^{(n-1)}\right) = 6n - 16, \\ f\left(v_2^{(n-1)}\right) = 6n - 16, \\ f\left(v_2^{(\alpha)}\right) = 6\alpha - 5 \text{ for } 2 \le \alpha \le n - 2 \\ \text{and } f\left(v_2^{(n-1)}\right) = 6n - 14. \end{cases}$$
The induced edge labeling is as follows:

$$f^*(u_\alpha u_{\alpha+1}) = \begin{cases} 3 & \alpha = 1 \\ 6\alpha - 1 & \alpha = 1 \\ 6\alpha - 2 & \alpha = 1 \end{cases}$$

$$f^{*}(u_{\alpha}u_{\alpha+1}) = \begin{cases} 6\alpha - 4 & 2 \le \alpha \le n-3, \\ 6\alpha - 4 & 2 \le \alpha \le n-3, \end{cases}$$

$$f^{*}(u_{n-2}u_{n-1}) = 6n - 15, f^{*}(u_{n-1}u_{n}) = 6n - 10, \\ f^{*}(u_{\alpha}v_{1}^{(\alpha)}) = 6\alpha - 8 \text{ for } 2 \le \alpha \le n-2, \end{cases}$$

$$f^{*}(u_{n-1}v_{1}^{(n-1)}) = 6n - 13 \text{ and}$$

$$f^{*}(u_{i}v_{2}^{(\alpha)}) = 6\alpha - 6 \text{ for } 2 \le \alpha \le n-1.$$

Hence, f is a super exponential mean labeling of $TW(P_n)$. Thus the graph $TW(P_n)$ is a super exponential mean graph, for $n \ge 3$.

3 Conclusion

In this paper, the results on super exponential meanness of some standard graphs have been discussed. It is possible to investigate the super exponential meanness for other graphs.

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